

# Asymptotic Statistics

## Asymptotic Statistics Understanding Asymptotic Statistics: A Comprehensive Guide

Asymptotic statistics is a fundamental branch of statistical theory that deals with the behavior of estimators and test statistics as the sample size tends toward infinity. This area of study provides powerful tools for understanding the properties of statistical methods in large-sample contexts, offering insights that are often impractical to obtain through finite-sample analysis alone. Asymptotic techniques underpin many modern statistical procedures, including hypothesis testing, confidence interval construction, and the development of robust estimators. In the realm of statistical inference, exact finite-sample distributions are often complex or unknown, especially for intricate models or small datasets. Asymptotic methods circumvent these issues by analyzing the limiting behavior of estimators and test statistics, leading to simplified models and more manageable inferential procedures. This article explores the core concepts, key theorems, applications, and advantages of asymptotic statistics, providing a detailed overview for students, researchers, and practitioners alike.

**What Is Asymptotic Statistics?** Asymptotic statistics focuses on properties of statistical procedures as the sample size  $(n)$  approaches infinity. It examines how estimators behave, how test statistics distribute, and how inference can be improved when large datasets are available. Key ideas include:

- **Asymptotic consistency:** Ensuring estimators converge in probability to the true parameter value as  $(n \rightarrow \infty)$ .
- **Asymptotic normality:** Demonstrating that suitably normalized estimators tend toward a normal distribution in the limit.
- **Asymptotic efficiency:** Comparing estimators based on their limiting variances to determine which performs best for large samples. These concepts allow statisticians to develop approximate inference tools that are valid in large samples, even when exact finite-sample distributions are complex or unknown.

**Core Concepts in Asymptotic Statistics**

- 1. Consistency of Estimators** An estimator  $(\hat{\theta}_n)$  of a parameter  $(\theta)$  is said to be consistent if it converges in probability to the true parameter value as  $(n \rightarrow \infty)$ . Formally:  $\hat{\theta}_n \xrightarrow{p} \theta$

Consistency is a foundational property, ensuring that with sufficiently large data, the estimator approximates the true parameter accurately.

- 2. Asymptotic Normality** Many estimators, when properly scaled, tend to follow a normal distribution asymptotically. This property is crucial because it allows for approximate confidence intervals and hypothesis tests.

Typically, for an estimator  $(\hat{\theta}_n)$  of  $(\theta)$ , asymptotic normality is expressed as:  $\sqrt{n}(\hat{\theta}_n - \theta) \xrightarrow{d} N(0, V)$  where  $(V)$  is the asymptotic variance, and  $\xrightarrow{d}$  denotes convergence in distribution.

- 3. Asymptotic Efficiency** Among a class of estimators, one is asymptotically efficient if it achieves the lowest possible asymptotic variance, often corresponding to the Cramér-Rao lower bound. This concept guides the development of optimal estimators in large samples.

**Key Theorems and Results in Asymptotic Theory**

- 1. Law of Large Numbers (LLN)** The LLN states that the sample mean converges in probability to the population mean:  $\bar{X}_n \xrightarrow{p} \mu$  as  $(n \rightarrow \infty)$ . This is a foundational result underpinning many asymptotic analyses.

- 2. Central Limit Theorem (CLT)** The CLT provides the basis for asymptotic normality:  $\sqrt{n}(\bar{X}_n - \mu) \xrightarrow{d} N(0, \sigma^2)$

$\sigma^2]$  where  $(\sigma^2)$  is the population variance. 3. Asymptotic Distribution of Maximum Likelihood Estimators (MLEs) Under regularity conditions, MLEs are asymptotically normal:  $\sqrt{n}(\hat{\theta}_{MLE} - \theta) \xrightarrow{d} N(0, I(\theta)^{-1})$  where  $(I(\theta))$  is the Fisher information. 4. Taylor Expansion and Influence Functions These tools are used to derive the asymptotic distribution of estimators and to understand their robustness and efficiency. Applications of Asymptotic Statistics The principles of asymptotic statistics have widespread applications across various fields: 3.1. Hypothesis Testing Large-sample tests rely on asymptotic distributions. For example, the likelihood ratio test, Wald test, and score test often use asymptotic chi-square distributions to determine significance levels. 2. Confidence Intervals Asymptotic normality allows for the construction of approximate confidence intervals for parameters, especially when finite-sample distributions are unknown or complicated. 3. Estimation Procedures Many estimators, such as MLEs and method of moments estimators, are analyzed for their asymptotic properties to assess their efficiency and bias. 4. Model Selection and Evaluation Information criteria like AIC and BIC are based on asymptotic approximations of likelihood-based measures, guiding model choice in large datasets. Advantages of Asymptotic Methods - Simplification of complex models: Asymptotic results often lead to straightforward approximations that are easier to analyze and interpret. - Guidance for finite-sample inference: Although asymptotic results are valid only in large samples, they often provide reasonable approximations even with moderate sample sizes. - Development of optimal estimators: Asymptotic theory helps identify estimators with desirable properties, such as minimal variance. - Foundation for modern statistical methods: Many advanced techniques, including bootstrap and Bayesian asymptotics, build upon asymptotic principles. Limitations and Considerations While powerful, asymptotic methods have limitations: - Finite-sample accuracy: In small samples, asymptotic approximations may be inaccurate, leading to misleading inferences. - Regularity conditions: Asymptotic normality and efficiency often require assumptions about the data distribution and model regularity that may not hold in practice. - Model misspecification: Asymptotic results assume correct model specification; deviations can impact the validity of conclusions. Conclusion Asymptotic statistics serves as a cornerstone of modern statistical inference, providing 4 essential tools for understanding the behavior of estimators and test procedures in large samples. Its principles enable statisticians to develop, analyze, and improve methods for data analysis across diverse fields, from economics to biomedical sciences. While it has limitations, especially in finite samples, the insights gained through asymptotic analysis continue to influence the evolution of statistical theory and practice. Embracing asymptotic methods equips researchers with a deeper understanding of the properties and performance of statistical procedures, ultimately leading to more robust and reliable inferences in the age of big data.

**QuestionAnswer** What is asymptotic statistics and why is it important? Asymptotic statistics studies the properties of estimators and test statistics as the sample size tends to infinity. It is important because it provides approximate distributions and performance measures for statistical procedures in large samples, simplifying analysis and guiding practical decision-making. What are common asymptotic distributions used in statistics? Common asymptotic distributions include the normal distribution (via the Central Limit Theorem), chi-square distribution, t-distribution, and the F-distribution. These distributions describe the behavior of estimators and test statistics as sample sizes grow large. How does the Law of Large Numbers relate to asymptotic analysis?

The Law of Large Numbers states that sample averages converge to the true population mean as sample size increases, forming a foundation for asymptotic consistency of estimators. It highlights the behavior of estimates in large samples, which is a key focus of asymptotic statistics. What is the difference between asymptotic and finite-sample properties? Asymptotic properties describe the behavior of estimators and test statistics as sample size approaches infinity, often simplifying analysis. Finite-sample properties concern their performance with specific, limited sample sizes. Asymptotic results are approximations that become more accurate as samples grow large. What are some common methods used in asymptotic analysis? Common methods include Taylor series expansions, Slutsky's theorem, the delta method, and the use of limit theorems like the Central Limit Theorem. These tools help derive the asymptotic distribution of estimators and test statistics. Why is asymptotic normality a key concept in statistical inference? Asymptotic normality indicates that, under certain conditions, estimators or test statistics follow a normal distribution as the sample size increases. This allows statisticians to use normal distribution-based methods for inference, such as confidence intervals and hypothesis tests, in large samples. Asymptotic Statistics: A Deep Dive into Large Sample Theory Asymptotic statistics forms the backbone of modern statistical inference, providing powerful tools and approximations that enable statisticians to analyze the behavior of estimators and test statistics as the sample size grows large. This branch of statistics focuses on understanding the limiting properties of estimators, probabilities, and distributions as the number of observations approaches infinity. Its insights are fundamental for developing confidence intervals, hypothesis tests, and understanding the efficiency of estimators in large-sample contexts. In this comprehensive review, we explore the core concepts, important theorems, applications, and nuances of asymptotic statistics, aiming to equip readers with a thorough understanding of this vital area. --- Introduction to Asymptotic Statistics Asymptotic statistics is concerned with the properties of estimators, test procedures, and statistical models in the limit as the sample size  $\rightarrow \infty$ . Unlike finite-sample methods, which focus on exact distributions, asymptotic methods provide approximations that are often easier to analyze and compute, especially for complex models. Why is asymptotic analysis important? - Exact distributions of estimators or test statistics are often intractable or unknown. - Asymptotic results offer approximate distributions that are valid for large sample sizes. - They facilitate the derivation of properties like consistency, efficiency, and normality. - They underpin many modern statistical techniques, including maximum likelihood estimation, Bayesian asymptotics, and nonparametric methods. --- Fundamental Concepts in Asymptotic Theory Consistency of Estimators An estimator  $\hat{\theta}_n$  of a parameter  $\theta$  is consistent if it converges in probability to the true parameter value as the sample size increases:  $\hat{\theta}_n \xrightarrow{p} \theta$  as  $n \rightarrow \infty$ . Implication: For large samples, the estimator becomes arbitrarily close to the true parameter, ensuring reliability. Asymptotic Normality Many estimators, under regularity conditions, are approximately normally distributed for large  $n$ :  $\sqrt{n}(\hat{\theta}_n - \theta) \xrightarrow{d} N(0, \sigma^2)$ , where  $\sigma^2$  is the asymptotic variance. Significance: This property allows the use of normal distribution approximations to construct confidence intervals and perform hypothesis testing even when the exact distribution is unknown. Asymptotic Efficiency An estimator is asymptotically efficient if it achieves the lowest possible asymptotic variance, often attaining the Cramér-Rao lower bound. Key Point: Efficiency measures how well an estimator performs relative to the

best possible estimator in large samples. --- Asymptotic Statistics 6 Core Theorems in Asymptotic Statistics Law of Large Numbers (LLN) The LLN states that the sample mean converges in probability to the expected value:  $\bar{X}_n \xrightarrow{p} \mathbb{E}[X]$ . Role in Asymptotics: Establishes consistency of sample means and other estimators derived from averages. Central Limit Theorem (CLT) The CLT asserts that, for i.i.d. random variables with finite variance:  $\frac{\sum_{i=1}^n X_i - n\mu}{\sqrt{n}} \xrightarrow{d} N(0, 1)$ , where  $\mu = \mathbb{E}[X_i]$  and  $\sigma^2 = \operatorname{Var}(X_i)$ . Implication: Justifies the normal approximation for sums or averages of large samples. Asymptotic Distribution of Estimators Under regularity conditions, maximum likelihood estimators (MLEs) are asymptotically normal:  $\sqrt{n}(\hat{\theta}_n - \theta) \xrightarrow{d} N(0, I(\theta)^{-1})$ , where  $I(\theta)$  is the Fisher information. Utility: Enables approximation of the distribution of estimators for inference. --- Asymptotic Techniques and Methods Taylor Expansions Often used to derive the asymptotic distribution of estimators, especially MLEs, by expanding likelihood functions around the true parameter. Slutsky's Theorem Allows combining convergent sequences; if  $X_n \xrightarrow{d} X$  and  $Y_n \xrightarrow{p} c$ , then:  $X_n + Y_n \xrightarrow{d} X + c$ . In practice: Used to justify replacing consistent estimators with their limits in asymptotic distributions. Delta Method Provides the asymptotic distribution of functions of estimators:  $\sqrt{n}(g(\hat{\theta}_n) - g(\theta)) \xrightarrow{d} N(0, [g'(\theta)]^2 \sigma^2)$ , where  $g$  is differentiable at  $\theta$ . Application: Deriving asymptotic distributions of complex estimators or test statistics. --- Asymptotic Statistics 7 Types of Asymptotic Results Asymptotic Normality As previously discussed, many estimators are asymptotically normal, which simplifies inference in large samples. Asymptotic Chi-Square and Other Distributions Certain test statistics, such as likelihood ratio tests, Wald tests, and score tests, have asymptotic chi-square distributions under the null hypothesis. For example:  $2 \times \text{log-likelihood ratio} \xrightarrow{d} \chi^2_k$ , where  $k$  is the number of parameters tested. Asymptotic Equivalence Different estimators or test procedures may be asymptotically equivalent, meaning they converge to the same limiting distribution or value, which can justify substituting one method for another in large samples. --- Applications of Asymptotic Statistics Maximum Likelihood Estimation (MLE) - MLEs are often asymptotically efficient and normal. - Asymptotic theory enables approximation of the distribution of MLEs for constructing confidence intervals and hypothesis tests. - Regularity conditions ensure the validity of asymptotic normality. Hypothesis Testing - Asymptotic distributions, like chi-square, guide the development of tests such as likelihood ratio tests. - Large-sample approximations simplify calculations and improve test properties. Confidence Intervals - Asymptotic normality allows for constructing approximate confidence intervals based on the estimated standard error. Nonparametric and Semi-Parametric Methods - Asymptotics extend beyond parametric models, aiding in understanding the behavior of estimators like kernel density estimates, empirical processes, and rank-based procedures. --- Asymptotic Statistics 8 Nuances and Limitations of Asymptotic Theory - Finite Sample Limitations: Asymptotic results are approximations; their accuracy depends on the sample size. - Regularity Conditions: Many theorems require conditions like differentiability, identifiability, and finite Fisher information; violations can invalidate results. - Speed of Convergence: Some estimators converge slowly, limiting the usefulness of asymptotic approximations in small samples. - Model Misspecification: Asymptotic properties may not hold if the model assumptions are violated. --

- Advanced Topics in Asymptotic Statistics Empirical Process Theory Provides tools to analyze the asymptotic behavior of more complex estimators like nonparametric regression functions and density estimators. Semiparametric and Nonparametric Asymptotics - Focus on estimators that do not specify the entire data-generating process. - Asymptotic efficiency and convergence rates are crucial considerations. Bayesian Asymptotics - Studies the behavior of posterior distributions as data accumulates. - Key results include Bernstein–von Mises theorem, linking Bayesian and frequentist asymptotics. --- Conclusion Asymptotic statistics provides a vital framework for understanding the properties of statistical procedures in large samples. Its theorems and techniques underpin much of statistical theory and practice, enabling the development of estimators, tests, and models that are both practical and theoretically justified. While asymptotic results are approximations, their widespread applicability, simplicity, and deep insights make them indispensable in modern statistics. Mastery of asymptotic theory necessitates understanding its core principles, regularity conditions, and limitations, but doing so empowers statisticians to design robust procedures capable of leveraging large datasets effectively. As the volume of data continues to grow in the digital age, asymptotic statistics remains at the forefront of statistical research and application, ensuring that statistical inference remains feasible, accurate, and theoretically grounded in the face of increasingly complex data limit theorems, convergence in distribution, consistency, asymptotic normality, estimator properties, large sample theory, law of large numbers, central limit theorem, asymptotic Asymptotic Statistics 9 efficiency, statistical inference

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*Hajek J. Pfanzagl*

this accessible and easy to read book provides many examples to illustrate diverse topics in probability and statistics from initial concepts up to advanced calculations special attention is devoted e g to independency of events inequalities in probability and functions of random variables the book is directed to students of mathematics statistics engineering and other quantitative sciences in particular to readers who need or want to learn by self study the author is convinced that sophisticated examples are more useful for the student than a lengthy formalism treating the greatest possible generality contents mathematics revision introduction to probability finite sample spaces conditional probability and independence one dimensional random variables functions of random variables bi dimensional random variables characteristics of random variables discrete probability models continuous probability models generating functions in probability sums of many random variables samples and sampling distributions estimation of parameters hypothesis tests

this textbook is devoted to the general asymptotic theory of statistical experiments local asymptotics for statistical models in the sense of local asymptotic mixed normality or local asymptotic quadraticity make up the core of the book numerous examples deal with classical independent and identically distributed models and with stochastic processes the book can be read in different ways according to possibly different mathematical preferences of the reader one reader may focus on the statistical theory and thus on the chapters about gaussian shift models mixed normal and quadratic models and on local asymptotics where the limit model is a gaussian shift or a mixed normal or a quadratic experiment lan lamm laq another reader may prefer an introduction to stochastic process models where given statistical results apply and thus concentrate on subsections or chapters on likelihood ratio processes and some diffusion type models where lan lamm or laq occurs finally readers might put together both aspects the book is suitable for graduate students starting to work in statistics of stochastic processes as well as for researchers interested in a precise introduction to this area

this book is intended as an introduction to probability theory and mathematical statistics for students in mathematics the physical sciences engineering and related fields it is based on the author s 25 years of experience teaching probability and is squarely aimed at helping students overcome common difficulties in learning the subject the focus of the book is an explanation of the theory mainly by the use of many examples whenever possible proofs of stated results are provided all sections conclude with a short list of problems the book also includes several optional sections on more advanced topics this textbook would be ideal for use in a first course in probability theory contents probabilities conditional probabilities and independence random variables and their distribution operations on random variables expected value variance and covariance normally distributed random vectors limit theorems mathematical statistics appendix bibliography index

the idea of the book is to present a text that is useful for both students of quantitative sciences and practitioners who work with univariate or multivariate probabilistic models since the text should also be suitable for self study excessive formalism is avoided though mathematical rigor is retained a deeper insight into the topics is provided by detailed examples and illustrations the book covers the standard content of a course in probability and statistics

however the second edition includes two new chapters about distribution theory and exploratory data analysis the first mentioned chapter certainly goes beyond the standard material it is presented to reflect the growing practical importance of developing new distributions the second new chapter studies intensively one and bidimensional concepts like assymetry kurtosis correlation and determination coefficients in particular examples are intended to enable the reader to take a critical look at the appropriateness of the geometrically motivated concepts

change point analysis is a crucial statistical technique for detecting structural breaks within datasets applicable in diverse fields such as finance and weather forecasting the authors of this book aim to consolidate recent advancements and broaden the scope beyond traditional time series applications to include biostatistics longitudinal data analysis high dimensional data and network analysis the book introduces foundational concepts with practical data examples from literature alongside discussions of related machine learning topics subsequent chapters focus on mathematical tools for single and multiple change point detection along with statistical inference issues which provide rigorous proofs to enhance understanding but assume readers have foundational knowledge in graduate level probability and statistics the book also expands the discussion into threshold regression frameworks linked to subgroup identification in modern statistical learning and apply change point analysis to functional data and dynamic networks areas not comprehensively covered elsewhere key features comprehensive coverage of diverse applications this book expands the scope of change point analysis to include biostatistics longitudinal data high dimensional data and network analysis this broad applicability makes it a valuable resource for researchers and students across various disciplines integration of theory and practice the book balances rigorous mathematical theory with practical applications by providing extensive computational examples using r each chapter features real world data illustrations and discussions of relevant machine learning topics ensuring that readers can see the relevance of theoretical concepts in applied settings accessibility for students the content is designed with graduate level students in mind providing clear explanations and structured guidance through complex mathematical tools rigorous proofs are included to facilitate understanding without overwhelming readers with overly advanced theories early on the book incorporates computational results using r showcasing various packages tailored for specific methods or problem domains while providing references for further exploration by offering a selection of widely adopted methodologies relevant in scientific research as well as business contexts this text aims to equip junior researchers with essential tools needed for their work in change point analysis

this book provides a technical and specialised discussion of contemporary and emerging issues in foreign exchange and financial markets by addressing the issues of risk management and theory and hypothesis development which have general implications for finance theory and foreign exchange market management it offers an in depth comprehensive analysis of the issues concerning the volatility of exchange rates the book has three main objectives first it applies the integrated study of exchange rate volatility in terms of depth and breadth second it applies the integrated study of exchange rate volatility in malaysia as a case study of a developing country malaysia had imposed capital control measures in the past and has now liberalised its exchange rate market and will continue to liberalise it further in the

long run hence the need to understand exchange rate volatility measurement and management will be even more important in the future third the book highlights new conditional volatility models for a developing country such as malaysian and develops advanced econometric models which have produced results for sound risk management strategies and for achieving risk management in the financial market and the economy additionally the authors recommend risk management themes which may be of relevance to other developing countries this work can be used as a reference book by fund managers financial market analysts researchers academics practitioners policy makers and postgraduate students in the areas of finance accounting business and financial economics it can also be a supplementary text for ph d and masters students in these areas

in the summer of 1968 one of the present authors llc had the pleasure of giving a sequence of lectures at the university of mon treal lecture notes were collected and written out by drs catherine doleans jean haezendonck and roch roy they were published in french by the presses of the university of montreal as part of their series of seminaires de mathematiques superieures twenty years later it was decided that a chinese translation could be useful but upon prodding by professor shanti gupta at purdue we concluded that the notes should be updated and rewritten in english and in chinese the present volume is the result of that effort we have preserved the general outline of the lecture notes but we have deleted obsolete material and sketched some of the results acquired during the past twenty years this means that while the original notes concentrated on the lan situation we have included here some results of jeganathan and others on the lamm case also included are versions of the hajek le cam asymptotic minimax and convolution theorems with some of their implications we have not attempted to give complete coverage of the subject and have often stated theorems without indicating their proofs

this book developed out of my year long course on asymptotic theory at purdue university to some extent the topics coincide with what i cover in that course there are already a number of well known books on asy totics this book is quite different it covers more topics in one source than are available in any other single book on asymptotic theory numerous topics covered in this book are available in the literature in a scattered manner and they are brought together under one umbrella in this book asymptotic theory is a central unifying theme in probability and statistics my main goal in writing this book is to give its readers a feel for the incredible scope and reach of asymptotics i have tried to write this book in a way that is accessible and to make the reader appreciate the beauty of theory and the insights that only theory can provide essentially every theorem in the book comes with at least one reference preceding or following the statement of the theorem in addition i have provided a separate theorem by theorem reference as an entry on its own in the front of the book to make it extremely convenient for the reader to find a proof that was not provided in the text also particularly worth mentioning is a collection of nearly 300 practically useful inequalities that i have collected together from numerous sources this is appended at the very end of the book

traditions of the 150 year old st petersburg school of probability and statistics had been developed by many prominent scientists including p l chebychev a m lyapunov a a markov s n bernstein and yu v linnik in 1948 the chair of probability and statistics was established at the department of mathematics and mechanics of the st petersburg state university with yu v linnik

being its founder and also the first chair nowadays alumni of this chair are spread around russia lithuania france germany sweden china the united states and canada the fiftieth anniversary of this chair was celebrated by an international conference which was held in st petersburg from june 24 28 1998 more than 125 probabilists and statisticians from 18 countries azerbaijan canada finland france germany hungary israel italy lithuania the netherlands norway poland russia taiwan turkey ukraine uzbekistan and the united states participated in this international conference in order to discuss the current state and perspectives of probability and mathematical statistics the conference was organized jointly by st petersburg state university st petersburg branch of mathematical institute and the euler institute and was partially sponsored by the russian foundation of basic researches the main theme of the conference was chosen in the tradition of the st

the book presents the fundamental concepts from asymptotic statistical inference theory elaborating on some basic large sample optimality properties of estimators and some test procedures the most desirable property of consistency of an estimator and its large sample distribution with suitable normalization are discussed the focus being on the consistent and asymptotically normal can estimators it is shown that for the probability models belonging to an exponential family and a cramer family the maximum likelihood estimators of the indexing parameters are can the book describes some large sample test procedures in particular the most frequently used likelihood ratio test procedure various applications of the likelihood ratio test procedure are addressed when the underlying probability model is a multinomial distribution these include tests for the goodness of fit and tests for contingency tables the book also discusses a score test and wald s test their relationship with the likelihood ratio test and karl pearson s chi square test an important finding is that while testing any hypothesis about the parameters of a multinomial distribution a score test statistic and karl pearson s chi square test statistic are identical numerous illustrative examples of differing difficulty level are incorporated to clarify the concepts for better assimilation of the notions various exercises are included in each chapter solutions to almost all the exercises are given in the last chapter to motivate students towards solving these exercises and to enable digestion of the underlying concepts the concepts from asymptotic inference are crucial in modern statistics but are difficult to grasp in view of their abstract nature to overcome this difficulty keeping up with the recent trend of using r software for statistical computations the book uses it extensively for illustrating the concepts verifying the properties of estimators and carrying out various test procedures the last section of the chapters presents r codes to reveal and visually demonstrate the hidden aspects of different concepts and procedures augmenting the theory with r software is a novel and a unique feature of the book the book is designed primarily to serve as a text book for a one semester introductory course in asymptotic statistical inference in a post graduate program such as statistics bio statistics or econometrics it will also provide sufficient background information for studying inference in stochastic processes the book will cater to the need of a concise but clear and student friendly book introducing conceptually and computationally basics of asymptotic inference

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## FAQs

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