

EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY SOLUTIONS

EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY SOLUTIONS

EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY SOLUTIONS UNLOCKING THE SECRETS OF SHAPE AND SPACE GEOMETRY

THE VERY WORD CONJURES IMAGES OF INTRICATE DIAGRAMS PERPLEXING PROOFS AND THE SATISFYING CLICK OF UNDERSTANDING WHEN A COMPLEX PROBLEM FINALLY YIELDS ITS SOLUTION

FOR CENTURIES MATHEMATICIANS HAVE GRAPPLED WITH THE ELEGANT MYSTERIES OF SHAPE AND SPACE BUILDING UPON THE FOUNDATIONS LAID BY EUCLID HIMSELF

BUT GEOMETRY ISNT JUST AN ABSTRACT ACADEMIC PURSUIT ITS THE BACKBONE OF COUNTLESS TECHNOLOGIES FROM ARCHITECTURAL MARVELS TO THE SOPHISTICATED ALGORITHMS DRIVING OUR SMARTPHONES

THIS JOURNEY DELVES INTO THE FASCINATING WORLDS OF EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY OFFERING SOLUTIONS AND ILLUMINATING THEIR PRACTICAL APPLICATIONS

IMAGINE A WORLD WITHOUT PRECISE MEASUREMENTS

BUILDINGS WOULD CRUMBLE BRIDGES WOULD COLLAPSE AND EVEN THE SIMPLEST MACHINE WOULD FAIL

THIS IS WHERE EUCLIDEAN GEOMETRY STEPS IN ITS CRISP LINES AND RIGOROUS LOGIC PROVIDING THE FRAMEWORK FOR OUR PHYSICAL REALITY

EUCLIDEAN GEOMETRY NAMED AFTER THE ANCIENT GREEK MATHEMATICIAN EUCLID RELIES ON AXIOMS SELF EVIDENT TRUTHS TO BUILD A SYSTEM OF THEOREMS AND PROOFS

ITS THE GEOMETRY OF STRAIGHT LINES FLAT PLANES AND CONSTANT ANGLES

THE GEOMETRY WE INTUITIVELY UNDERSTAND WHEN WE MEASURE A ROOM OR DRAW A PERFECT SQUARE

THINK OF A PERFECTLY CRAFTED WOODEN TABLE

ITS LEGS METICULOUSLY ALIGNED FORM RIGHT ANGLES WITH THE TABLETOP

THE TABLETOP ITSELF A FLAT PLANE IS A TESTAMENT TO EUCLIDEAN PRINCIPLES

EVEN THE SLIGHT IMPERFECTIONS A SLIGHTLY UNEVEN LEG A TINY WARP IN THE WOOD HIGHLIGHT THE IDEALIZED PERFECTION THAT EUCLIDEAN GEOMETRY STRIVES FOR

SOLVING PROBLEMS IN EUCLIDEAN GEOMETRY OFTEN INVOLVES APPLYING THEOREMS LIKE PYTHAGORAS THEOREM A B C OR TRIGONOMETRIC IDENTITIES TO CALCULATE DISTANCES ANGLES AND AREAS

FOR INSTANCE DETERMINING THE HEIGHT OF A TALL BUILDING USING ITS SHADOW AND THE ANGLE OF ELEVATION IS A CLASSIC APPLICATION OF EUCLIDEAN PRINCIPLES

HOWEVER THE WORLD ISNT ALWAYS AS NEAT AND TIDY AS EUCLIDEAN GEOMETRY SUGGESTS

CONSIDER A CRUMPLED PIECE OF PAPER

ITS SURFACE IS NO LONGER A FLAT PLANE

ITS WARPED AND DISTORTED

THIS IS WHERE TRANSFORMATIONAL GEOMETRY ENTERS THE SCENE

EXTENDING THE BOUNDARIES OF EUCLIDEAN GEOMETRY TO ENCOMPASS SHAPES IN MOTION AND SHAPES THAT UNDERGO TRANSFORMATIONS

TRANSFORMATIONAL GEOMETRY DEALS WITH THE CHANGES IN SHAPES AND THEIR PROPERTIES UNDER VARIOUS TRANSFORMATIONS SUCH AS ROTATIONS TRANSLATIONS REFLECTIONS AND DILATIONS

IMAGINE A KALEIDOSCOPE

THE INTRICATE PATTERNS CREATED ARE A BEAUTIFUL REPRESENTATION OF TRANSFORMATIONAL GEOMETRY

EACH SYMMETRICAL IMAGE IS A REFLECTION A ROTATION OR A COMBINATION OF BOTH APPLIED REPEATEDLY TO A SIMPLE BASE PATTERN

SIMILARLY COMPUTER GRAPHICS RELY HEAVILY ON TRANSFORMATIONAL GEOMETRY TO MANIPULATE AND RENDER IMAGES

ROTATING A 3D MODEL ZOOMING IN OR OUT OR EVEN SUBTLY WARPING AN IMAGE FOR ARTISTIC EFFECT

ALL ARE ACCOMPLISHED USING THE PRINCIPLES OF TRANSFORMATIONAL GEOMETRY

SOLVING PROBLEMS IN TRANSFORMATIONAL GEOMETRY OFTEN INVOLVES UNDERSTANDING THE PROPERTIES THAT REMAIN INVARIANT UNCHANGED UNDER SPECIFIC TRANSFORMATIONS

FOR EXAMPLE THE DISTANCE BETWEEN TWO POINTS REMAINS UNCHANGED UNDER A TRANSLATION SHIFTING OR A ROTATION

WHILE THE AREA OF A SHAPE MIGHT CHANGE UNDER A DILATION SCALING

UNDERSTANDING THESE INVARIANTS ALLOWS US TO PREDICT THE OUTCOME OF TRANSFORMATIONS AND TO SOLVE PROBLEMS INVOLVING CONGRUENT SHAPES OR SIMILAR SHAPES

BRIDGING THE GAP WHILE DISTINCT EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY ARE DEEPLY INTERTWINED

EUCLIDEAN GEOMETRY PROVIDES THE FOUNDATIONAL FRAMEWORK FOR UNDERSTANDING SHAPES AND THEIR PROPERTIES WHILE TRANSFORMATIONAL GEOMETRY EXTENDS THIS UNDERSTANDING TO DYNAMIC SITUATIONS AND MORE COMPLEX SHAPES

MANY

PROBLEMS REQUIRE A COMBINED APPROACH USING EUCLIDEAN METHODS TO ANALYZE THE INITIAL STATE OF A SHAPE AND TRANSFORMATIONAL METHODS TO ANALYZE ITS CHANGES UNDER DIFFERENT CONDITIONS. REAL WORLD APPLICATIONS THE APPLICATIONS OF BOTH EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY ARE VAST AND PROFOUND. ARCHITECTURE AND ENGINEERING DESIGNING BUILDINGS, BRIDGES AND OTHER STRUCTURES REQUIRES PRECISE MEASUREMENTS AND CALCULATIONS BASED ON EUCLIDEAN GEOMETRY. TRANSFORMATIONAL GEOMETRY IS CRUCIAL IN COMPUTER-AIDED DESIGN (CAD) SOFTWARE, COMPUTER GRAPHICS AND ANIMATION. CREATING REALISTIC AND ENGAGING VISUALS FOR VIDEO GAMES, MOVIES AND SIMULATIONS RELIES HEAVILY ON TRANSFORMATIONAL GEOMETRY TO MANIPULATE AND RENDER 3D MODELS. ROBOTICS AND AUTOMATION PROGRAMMING ROBOTS TO NAVIGATE AND MANIPULATE OBJECTS REQUIRES A DEEP UNDERSTANDING OF BOTH EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY TO CALCULATE POSITIONS, ORIENTATIONS AND MOVEMENTS. CARTOGRAPHY AND MAPPING CREATING ACCURATE MAPS INVOLVES USING GEOMETRIC PRINCIPLES TO PROJECT THE CURVED SURFACE OF THE EARTH ONTO A FLAT SURFACE. A PROCESS THAT INCORPORATES BOTH EUCLIDEAN AND NON-EUCLIDEAN GEOMETRIC CONCEPTS. MEDICAL IMAGING TECHNIQUES LIKE MRI AND CT SCANS USE GEOMETRIC PRINCIPLES TO CREATE THREE-DIMENSIONAL REPRESENTATIONS OF INTERNAL ORGANS WHICH ARE THEN MANIPULATED AND ANALYZED USING TRANSFORMATIONAL GEOMETRY. ACTIONABLE TAKEAWAYS: MASTER THE FUNDAMENTALS. A SOLID GRASP OF BASIC EUCLIDEAN GEOMETRY CONCEPTS IS CRUCIAL BEFORE TACKLING TRANSFORMATIONAL GEOMETRY. PRACTICE, PRACTICE, PRACTICE! SOLVING A WIDE RANGE OF PROBLEMS IS KEY TO DEVELOPING INTUITION AND PROBLEM-SOLVING SKILLS IN BOTH AREAS. VISUALIZE DRAWING DIAGRAMS AND VISUALIZING THE SHAPES AND TRANSFORMATIONS CAN GREATLY AID IN UNDERSTANDING AND SOLVING PROBLEMS. UTILIZE TECHNOLOGY EXPLORE GEOMETRY SOFTWARE AND ONLINE RESOURCES TO ENHANCE LEARNING AND VISUALIZATION. CONNECT TO REAL WORLD APPLICATIONS RELATING THE CONCEPTS TO REAL WORLD SCENARIOS MAKES LEARNING MORE ENGAGING AND MEANINGFUL.

FREQUENTLY ASKED QUESTIONS (FAQs)

1. WHAT IS THE DIFFERENCE BETWEEN EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY? EUCLIDEAN GEOMETRY DEALS WITH STATIC SHAPES AND THEIR PROPERTIES WHILE TRANSFORMATIONAL GEOMETRY FOCUSES ON HOW SHAPES CHANGE UNDER VARIOUS TRANSFORMATIONS.
2. IS NON-EUCLIDEAN GEOMETRY RELEVANT TO THIS DISCUSSION? WHILE WE FOCUSED ON EUCLIDEAN AND TRANSFORMATIONAL GEOMETRIES, NON-EUCLIDEAN GEOMETRIES LIKE SPHERICAL GEOMETRY EXIST AND ARE CRUCIAL IN FIELDS LIKE COSMOLOGY AND GPS TECHNOLOGY. THEY ARE BEYOND THE SCOPE OF THIS ARTICLE BUT REPRESENT IMPORTANT EXTENSIONS OF GEOMETRIC PRINCIPLES.
3. WHICH GEOMETRY IS MORE IMPORTANT? BOTH ARE CRUCIAL. EUCLIDEAN PROVIDES THE FOUNDATION WHILE TRANSFORMATIONAL EXTENDS ITS CAPABILITIES TO DYNAMIC SYSTEMS. THEIR INTERPLAY IS VITAL FOR MANY APPLICATIONS.
4. WHERE CAN I FIND MORE RESOURCES TO LEARN ABOUT GEOMETRY? NUMEROUS ONLINE RESOURCES, TEXTBOOKS AND EDUCATIONAL VIDEOS ARE AVAILABLE. SEARCH FOR EUCLIDEAN GEOMETRY TUTORIALS OR TRANSFORMATIONAL GEOMETRY EXAMPLES TO FIND SUITABLE LEARNING MATERIALS.
5. HOW CAN I IMPROVE MY PROBLEM-SOLVING SKILLS IN GEOMETRY? CONSISTENT PRACTICE, BREAKING DOWN COMPLEX PROBLEMS INTO SMALLER PARTS AND SEEKING HELP WHEN NEEDED ARE ALL VITAL STRATEGIES. WORKING WITH OTHERS AND EXPLAINING YOUR SOLUTIONS CAN ALSO ENHANCE UNDERSTANDING AND IMPROVE PROBLEM-SOLVING SKILLS.

GEOMETRY WHETHER EUCLIDEAN OR TRANSFORMATIONAL IS NOT JUST A COLLECTION OF FORMULAS AND THEOREMS. IT'S A LANGUAGE THAT DESCRIBES THE WORLD AROUND US. MASTERING THIS LANGUAGE UNLOCKS A DEEPER UNDERSTANDING OF THE UNIVERSE AND EMPOWERS US TO CREATE AND INNOVATE IN COUNTLESS WAYS. SO EMBRACE THE CHALLENGE, EXPLORE THE ELEGANCE AND UNLOCK THE SECRETS OF SHAPE AND SPACE.

EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY

EUCLIDEAN, NON-EUCLIDEAN, AND TRANSFORMATIONAL GEOMETRY

GEOMETRIC TRANSFORMATIONS

TRANSFORMATION GEOMETRY

EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY: A DEDUCTIVE INQUIRY

AN INTRODUCTION TO TRANSFORMATIONAL GEOMETRY

TRANSFORMATIONAL GEOMETRY

TRANSFORMATION GEOMETRY

GEOMETRY: AN INTEGRATED APPROACH

A COMPARATIVE REVIEW OF RECENT RESEARCHES IN GEOMETRY

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EUCLIDEAN GEOMETRY AND

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EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY EUCLIDEAN, NON-EUCLIDEAN, AND TRANSFORMATIONAL GEOMETRY GEOMETRIC TRANSFORMATIONS TRANSFORMATION GEOMETRY EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY: A DEDUCTIVE INQUIRY AN INTRODUCTION TO TRANSFORMATIONAL GEOMETRY TRANSFORMATIONAL GEOMETRY TRANSFORMATION GEOMETRY: AN INTEGRATED APPROACH A COMPARATIVE REVIEW OF RECENT RESEARCHES IN GEOMETRY TRANSFORMATION GEOMETRY THE COLLECTED MATHEMATICAL PAPERS OF ARTHUR CAYLEY ... BULLETIN (NEW SERIES) OF THE AMERICAN MATHEMATICAL SOCIETY BULLETIN OF THE NEW YORK MATHEMATICAL SOCIETY EUCLIDEAN GEOMETRY AND TRANSFORMATIONS SMITH'S MATHEMATICS TRANSFORMATIONAL PLANE GEOMETRY DIRECTORY WITH REGULATIONS FOR ESTABLISHING AND CONDUCTING SCIENCE SCHOOLS & CLASSES DIRECTORY, WITH REGULATIONS FOR ESTABLISHING AND CONDUCTING SCIENCE AND ART SCHOOLS AND CLASSES JOURNAL FOR RESEARCH IN MATHEMATICS EDUCATION SHLOMO LIBESKIND SHLOMO LIBESKIND R. zvan GELCA GEORGE E. MARTIN SHLOMO LIBESKIND FRANK M. ECCLES RICHARD G. BROWN MAX JAGER McDougal Littell Incorporated FELIX KLEIN MAX JEGER ARTHUR CAYLEY CLAYTON W. DODGE ROBERTO SMITH RONALD N. UMBLE EDUCATION MINISTRY OF

IDEAL FOR MATHEMATICS MAJORS AND PROSPECTIVE SECONDARY SCHOOL TEACHERS EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY PROVIDES A COMPLETE AND SOLID PRESENTATION OF EUCLIDEAN GEOMETRY WITH AN EMPHASIS ON SOLVING CHALLENGING PROBLEMS THE AUTHOR EXAMINES VARIOUS STRATEGIES AND HEURISTICS FOR APPROACHING PROOFS AND DISCUSSES THE PROCESS STUDENTS SHOULD FOLLOW TO DETERMINE HOW TO PROCEED FROM ONE STEP TO THE NEXT THROUGH NUMEROUS PROBLEM SOLVING TECHNIQUES A LARGE COLLECTION OF PROBLEMS VARYING IN LEVEL OF DIFFICULTY ARE INTEGRATED THROUGHOUT THE TEXT AND SUGGESTED HINTS FOR THE MORE CHALLENGING PROBLEMS APPEAR IN THE INSTRUCTOR'S SOLUTIONS MANUAL AND CAN BE USED AT THE INSTRUCTOR'S DISCRETION

THIS UNDERGRADUATE TEXTBOOK PROVIDES A COMPREHENSIVE TREATMENT OF EUCLIDEAN AND TRANSFORMATIONAL GEOMETRIES SUPPLEMENTED BY SUBSTANTIAL DISCUSSIONS OF TOPICS FROM VARIOUS NON EUCLIDEAN AND LESS COMMONLY TAUGHT GEOMETRIES MAKING IT IDEAL FOR BOTH MATHEMATICS MAJORS AND PRE SERVICE TEACHERS EMPHASIS IS PLACED ON DEVELOPING STUDENTS DEDUCTIVE REASONING SKILLS AS THEY ARE GUIDED THROUGH PROOFS CONSTRUCTIONS AND SOLUTIONS TO PROBLEMS THE TEXT FREQUENTLY EMPHASIZES STRATEGIES AND HEURISTICS OF PROBLEM SOLVING INCLUDING CONSTRUCTING PROOFS WHERE TO BEGIN HOW TO PROCEED WHICH APPROACH IS MORE PROMISING ARE THERE MULTIPLE SOLUTIONS PROOFS ETC THIS APPROACH AIMS NOT ONLY TO ENABLE STUDENTS TO SUCCESSFULLY SOLVE UNFAMILIAR PROBLEMS ON THEIR OWN BUT ALSO TO IMPART A LASTING APPRECIATION FOR MATHEMATICS THE TEXT FIRST EXPLORES AT A HIGHER LEVEL AND IN MUCH GREATER DEPTH TOPICS THAT ARE NORMALLY TAUGHT IN HIGH SCHOOL GEOMETRY COURSES DEFINITIONS AND AXIOMS CONGRUENCE CIRCLES AND RELATED CONCEPTS AREA AND THE PYTHAGOREAN THEOREM SIMILARITY ISOMETRIES AND SIZE TRANSFORMATIONS AND COMPOSITION OF TRANSFORMATIONS CONSTRUCTIONS AND THE USE OF TRANSFORMATIONS TO CARRY OUT CONSTRUCTIONS ARE EMPHASIZED THE TEXT THEN INTRODUCES MORE ADVANCED TOPICS DEALING WITH NON EUCLIDEAN AND LESS COMMONLY TAUGHT TOPICS SUCH AS INVERSIVE HYPERBOLIC ELLIPTIC TAXICAB FRACTAL AND SOLID GEOMETRIES BY EXAMINING WHAT HAPPENS WHEN ONE OR MORE OF THE BUILDING BLOCKS OF EUCLIDEAN GEOMETRY ARE ALTERED STUDENTS WILL GAIN A DEEPER UNDERSTANDING OF AND APPRECIATION FOR EUCLIDEAN CONCEPTS

TO ACCOMMODATE STUDENTS WITH DIFFERENT LEVELS OF EXPERIENCE IN THE SUBJECT THE BASIC DEFINITIONS AND AXIOMS THAT FORM THE FOUNDATION OF EUCLIDEAN GEOMETRY ARE COVERED IN CHAPTER 1 PROBLEM SETS ARE PROVIDED AFTER EVERY SECTION IN EACH CHAPTER AND INCLUDE NONROUTINE PROBLEMS THAT STUDENTS WILL ENJOY EXPLORING WHILE NOT NECESSARILY REQUIRED THE APPROPRIATE USE OF FREELY AVAILABLE DYNAMIC GEOMETRY SOFTWARE AND OTHER SPECIALIZED SOFTWARE REFERENCED IN THE TEXT IS STRONGLY ENCOURAGED THIS IS ESPECIALLY IMPORTANT FOR VISUAL LEARNERS AND FOR FORMING CONJECTURES AND TESTING HYPOTHESES

THIS TEXTBOOK TEACHES THE TRANSFORMATIONS OF PLANE EUCLIDEAN GEOMETRY THROUGH PROBLEMS OFFERING A TRANSFORMATION BASED PERSPECTIVE ON PROBLEMS THAT HAVE APPEARED IN RECENT YEARS AT MATHEMATICS COMPETITIONS AROUND THE GLOBE AS WELL AS ON SOME CLASSICAL EXAMPLES AND THEOREMS IT IS BASED ON THE COMBINED TEACHING EXPERIENCE OF THE AUTHORS COACHES OF SEVERAL MATHEMATICAL OLYMPIAD TEAMS IN BRAZIL ROMANIA AND THE USA AND PRESENTS COMPREHENSIVE THEORETICAL DISCUSSIONS OF ISOMETRIES HOMOTHETIES AND SPIRAL SIMILARITIES AND INVERSIONS ALL ILLUSTRATED BY EXAMPLES AND FOLLOWED BY MYRIAD PROBLEMS LEFT FOR THE READER TO SOLVE THESE PROBLEMS WERE CAREFULLY SELECTED AND ARRANGED TO INTRODUCE STUDENTS TO THE TOPICS BY GRADUALLY MOVING FROM BASIC TO EXPERT LEVEL MOST OF THEM HAVE APPEARED IN COMPETITIONS SUCH AS MATHEMATICAL OLYMPIADS OR IN MATHEMATICAL JOURNALS AIMED AT AN AUDIENCE INTERESTED IN MATHEMATICS COMPETITIONS WHILE SOME ARE FUNDAMENTAL FACTS OF MATHEMATICS DISCUSSED IN THE FRAMEWORK OF GEOMETRIC TRANSFORMATIONS THE BOOK OFFERS A GLOBAL VIEW OF THE GEOMETRIC CONTENT OF TODAY S MATHEMATICS COMPETITIONS BRINGING MANY NEW METHODS AND IDEAS TO THE ATTENTION OF THE PUBLIC TALENTED HIGH SCHOOL AND MIDDLE SCHOOL STUDENTS SEEKING TO IMPROVE THEIR PROBLEM SOLVING SKILLS CAN BENEFIT FROM THIS BOOK AS WELL AS HIGH SCHOOL AND COLLEGE INSTRUCTORS WHO WANT TO ADD NONSTANDARD QUESTIONS TO THEIR COURSES PEOPLE WHO ENJOY SOLVING ELEMENTARY MATH PROBLEMS AS A HOBBY WILL ALSO ENJOY THIS WORK

TRANSFORMATION GEOMETRY IS A RELATIVELY RECENT EXPRESSION OF THE SUCCESSFUL VENTURE OF BRINGING TOGETHER GEOMETRY AND ALGEBRA THE NAME DESCRIBES AN APPROACH AS MUCH AS THE CONTENT OUR SUBJECT IS EUCLIDEAN GEOMETRY ESSENTIAL TO THE STUDY OF THE PLANE OR ANY MATHEMATICAL SYSTEM IS AN UNDER STANDING OF THE TRANSFORMATIONS ON THAT SYSTEM THAT PRESERVE DESIGNATED FEATURES OF THE SYSTEM OUR STUDY OF THE AUTOMORPHISMS OF THE PLANE AND OF SPACE IS BASED ON ONLY THE MOST ELEMENTARY HIGH SCHOOL GEOMETRY IN PARTICULAR GROUP THEORY IS NOT A PREREQUISITE HERE ON THE CONTRARY THIS MODERN APPROACH TO EUCLIDEAN GEOMETRY GIVES THE CONCRETE EXAMPLES THAT ARE NECESSARY TO APPRECIATE AN INTRODUCTION TO GROUP THEORY THEREFORE A COURSE BASED ON THIS TEXT IS AN EXCELLENT PREREQUISITE TO THE STANDARD COURSE IN ABSTRACT ALGEBRA TAKEN BY EVERY UNDERGRADUATE MATHEMATICS MAJOR AN ADVANTAGE OF HAVING NB COLLEGE MATHEMATICS PREREQUISITE TO OUR STUDY IS THAT THE TEXT IS THEN USEFUL FOR GRADUATE MATHEMATICS COURSES DESIGNED FOR SECONDARY TEACHERS MANY OF THE STUDENTS IN THESE CLASSES EITHER HAVE NEVER TAKEN LINEAR ALGEBRA OR ELSE HAVE TAKEN IT TOO LONG AGO TO RECALL EVEN THE BASIC IDEAS IT TURNS OUT THAT VERY LITTLE IS LOST HERE BY NOT ASSUMING LINEAR ALGEBRA A PRELIMINARY VERSION OF THE TEXT WAS WRITTEN FOR AND USED IN TWO COURSES ONE WAS A GRADUATE COURSE FOR TEACHERS AND THE OTHER A SOPHOMORE COURSE DESIGNED FOR THE PROSPECTIVE TEACHER AND THE GENERAL MATHEMATICS MAJOR TAKING ONE COURSE IN GEOMETRY

IDEAL FOR MATHEMATICS MAJORS AND PROSPECTIVE SECONDARY SCHOOL TEACHERS EUCLIDEAN AND TRANSFORMATIONAL GEOMETRY PROVIDES A COMPLETE AND SOLID PRESENTATION OF EUCLIDEAN GEOMETRY WITH AN EMPHASIS ON SOLVING CHALLENGING PROBLEMS THE AUTHOR EXAMINES VARIOUS STRATEGIES AND HEURISTICS FOR APPROACHING PROOFS AND DISCUSSES THE PROCESS STUDENTS SHOULD FOLLOW TO DETERMINE HOW TO PROCEED FROM ONE STEP TO

THE NEXT THROUGH NUMEROUS PROBLEM SOLVING TECHNIQUES A LARGE COLLECTION OF PROBLEMS VARYING IN LEVEL OF DIFFICULTY ARE INTEGRATED THROUGHOUT THE TEXT AND SUGGESTED HINTS FOR THE MORE CHALLENGING PROBLEMS APPEAR IN THE INSTRUCTOR S SOLUTIONS MANUAL AND CAN BE USED AT THE INSTRUCTOR S DISCRETION

THIS INTRODUCTION TO EUCLIDEAN GEOMETRY EMPHASIZES TRANSFORMATIONS PARTICULARLY ISOMETRIES AND SIMILARITIES SUITABLE FOR UNDERGRADUATE COURSES IT INCLUDES NUMEROUS EXAMPLES MANY WITH DETAILED ANSWERS 1972 EDITION

WRITTEN BY AUTHOR KARL SMITH THE STUDENT SURVIVAL AND SOLUTIONS MANUAL PROVIDES SURVIVAL HINTS AS WELL AS DETAILED AND COMPLETE SOLUTIONS TO THE ODD NUMBERED EXERCISES AND TEST QUESTIONS

DESIGNED FOR A ONE SEMESTER COURSE AT THE JUNIOR UNDERGRADUATE LEVEL TRANSFORMATIONAL PLANE GEOMETRY TAKES A HANDS ON INTERACTIVE APPROACH TO TEACHING PLANE GEOMETRY THE BOOK IS SELF CONTAINED DEFINING BASIC CONCEPTS FROM LINEAR AND ABSTRACT ALGEBRA GRADUALLY AS NEEDED THE TEXT ADHERES TO THE NATIONAL COUNCIL OF TEACHERS OF MATHEMATICS PRINCIPLES AND STANDARDS FOR SCHOOL MATHEMATICS AND THE COMMON CORE STATE STANDARDS INITIATIVE STANDARDS FOR MATHEMATICAL PRACTICE FUTURE TEACHERS WILL ACQUIRE THE SKILLS NEEDED TO EFFECTIVELY APPLY THESE STANDARDS IN THEIR CLASSROOMS FOLLOWING FELIX KLEIN S ERLANGEN PROGRAM THE BOOK PROVIDES STUDENTS IN PURE MATHEMATICS AND STUDENTS IN TEACHER TRAINING PROGRAMS WITH A CONCRETE VISUAL ALTERNATIVE TO EUCLID S PURELY AXIOMATIC APPROACH TO PLANE GEOMETRY IT ENABLES GEOMETRICAL VISUALIZATION IN THREE WAYS KEY CONCEPTS ARE MOTIVATED WITH EXPLORATORY ACTIVITIES USING SOFTWARE SPECIFICALLY DESIGNED FOR PERFORMING GEOMETRICAL CONSTRUCTIONS SUCH AS GEOMETER S SKETCHPAD EACH CONCEPT IS INTRODUCED SYNTHETICALLY WITHOUT COORDINATES AND ANALYTICALLY WITH COORDINATES EXERCISES INCLUDE NUMEROUS GEOMETRIC CONSTRUCTIONS THAT USE A REFLECTING INSTRUMENT SUCH AS A MIRA AFTER REVIEWING THE ESSENTIAL PRINCIPLES OF CLASSICAL EUCLIDEAN GEOMETRY THE BOOK COVERS GENERAL TRANSFORMATIONS OF THE PLANE WITH PARTICULAR ATTENTION TO TRANSLATIONS ROTATIONS REFLECTIONS STRETCHES AND THEIR COMPOSITIONS THE AUTHORS APPLY THESE TRANSFORMATIONS TO STUDY CONGRUENCE SIMILARITY AND SYMMETRY OF PLANE FIGURES AND TO CLASSIFY THE ISOMETRIES AND SIMILARITIES OF THE PLANE

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